

**Ferrari, P. A.; Galves, A.; Liggett, T. M.**

**Exponential waiting time for filling a large interval in the symmetric simple exclusion process.** (English) [Zbl 0819.60095](#)

*Ann. Inst. Henri Poincaré, Probab. Stat.* 31, No. 1, 155-175 (1995).

The one-dimensional Markovian process with the nearest neighbor interaction is considered, i.e. the state space of the process is a collection of subsets in  $\mathbb{Z}$ . Probabilistic measure of the process is defined by means of the following condition. Let  $\mathbb{A} \subseteq \mathbb{Z}$  be the random state at time  $t$  and  $\mathbb{A}' \subseteq \mathbb{Z}$  be a state at time  $t + \Delta$ . Then the conditional probabilities of the transitions  $\mathbb{A} \rightarrow \mathbb{A}'$  are equal to each other if  $\mathbb{A}'$  differs from  $\mathbb{A}$  by the variation of the  $\mathbb{A}$ -neighbors. Namely, if both nearest neighbors  $x, y$  are contained in  $\mathbb{A}$ , then  $x, y \in \mathbb{A}'$ ; if  $x, y$  are not contained in  $\mathbb{A}$ , then  $x, y \notin \mathbb{A}'$  and if  $x \in \mathbb{A}, y \notin \mathbb{A}$ , then  $x \notin \mathbb{A}', y \in \mathbb{A}'$ . In other cases the variation rate is equal to zero. Such random process is called a symmetric simple exclusion one. The extremal invariant measures for this process are the product measure  $(\nu_\rho)^\mathbb{Z}$ ,  $\rho \in [0, 1]$ , and  $\nu_\rho$  is such that the site  $x \in \mathbb{Z}$  is occupied with the probability  $\rho$ . Let  $T_N$  be the first time that the sites  $\{1, 2, \dots, N\}$  get occupied, i.e.  $\{1, 2, \dots, N\} \subset \mathbb{A}$ . The following statement is proved: There exist  $0 < \alpha' \leq \alpha_N \leq \alpha'' < \infty$  and positive  $A$  and  $A'$  such that

$$\sup_{t \geq 0} |\mathbb{P}\{\alpha_N \rho^N T_N > t\} - e^{-t}| < A \rho^{A'N}.$$

Reviewer: [Y.P.Virchenko \(Khar'kov\)](#)

**MSC:**

- 60K35** Interacting random processes; statistical mechanics type models; percolation theory
- 82C22** Interacting particle systems in time-dependent statistical mechanics
- 60F10** Large deviations

Cited in **3** Documents

**Keywords:**

symmetric exclusion process; occurrence time of a rare event; large deviations

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