

**Grassi, Michele**

**Self-dual manifolds and mirror symmetry for the quintic threefold.** (English) Zbl 1085.14035  
*Asian J. Math.* 9, No. 1, 79-101 (2005).

The author describes a way to geometrically interpolate between the large Kähler structure limit of the Kähler moduli space of the anticanonical divisor in  $\mathbb{P}^n$  and a large complex structure limit of the complex structure moduli space of the mirror partner given by the *B. R. Greene, M. R. Plesser* orbifold construction [Duality in Calabi-Yau moduli space, *Nucl. Phys.* B338, 15–37 (1990)]. This is achieved by constructing a two-dimensional family of smooth manifolds  $\mathbb{X}_{\rho_1, \rho_2}$  of real dimension  $(3(n-1) + 2)$  endowed with a “weakly self-dual” (WSD) structure. A WSD structure consists of three closed 2-forms and a Riemannian metric satisfying certain integrability and compatibility conditions. Taking appropriate limiting values for  $\rho_1$  and  $\rho_2$ , the manifolds  $\mathbb{X}_{\rho_1, \rho_2}$  approach the large Kähler structure limit of the anticanonical divisor and the large complex structure limit of the mirror in a normalized Gromov-Hausdorff sense.

The construction starts with the fiber product  $(\mathbb{C}^*)^{n+1} \times_{\mu} (\mathbb{C}^*)^{n+1}$  over  $\mathbb{R}^{n+1}$ , where  $\mu : (\mathbb{C}^*)^{n+1} \rightarrow \mathbb{R}^{n+1}$  is the usual  $T^{n+1}$ -moment map given by rotating the coordinates. The WSD manifolds arise from a sort of “polysymplectic reduction” of  $(\mathbb{C}^*)^{n+1} \times_{\mu} (\mathbb{C}^*)^{n+1}$  by a group action arising from the reflexive polytope construction of  $\mathbb{P}^n$  and its toric dual.

Reviewer: [Edward Lee \(Los Angeles\)](#)

**MSC:**

[14J32](#) Calabi-Yau manifolds (algebraic-geometric aspects)  
[14M25](#) Toric varieties, Newton polyhedra, Okounkov bodies

Cited in **1** Review  
Cited in **3** Documents

**Keywords:**

[reflexive polytopes](#); [Gromov-Hausdorff distance](#)

**Full Text:** [DOI](#) [arXiv](#)