

**Shokurov, V. V.**

**The non-vanishing theorem.** (English. Russian original) [Zbl 0605.14006](#)

*Math. USSR, Izv.* 26, 591-604 (1986); translation from *Izv. Akad. Nauk SSSR, Ser. Mat.* 49, No. 3, 635-651 (1985).

The main result is the following non-vanishing theorem. Let  $X$  be a variety with routine (= log-terminal) singularities,  $D$  a nef (numerically effective) Cartier divisor and  $A = \sum d_i D_i^a$   $\mathbb{Q}$ -Cartier divisor on  $X$ . Suppose that the following conditions hold: (a) The  $\mathbb{Q}$ -divisor  $aD + A - K_X$  is nef and big for some  $a \in \mathbb{Q}$ . (b) The  $D_i$  are prime divisors on  $X$ , and are nonsingular, have normal crossings, and lie in the nonsingular part of  $X$  if  $d_i < 0$ . (c) Each  $d_i > -1$ . then for all  $b \gg 0$  :  $H^0(X, \mathcal{O}_X(bD + \lceil A \rceil)) \neq 0$ , or, in other words,  $|bD + \lceil A \rceil| \neq \emptyset$ , where for  $x \in \mathbb{R}$ , " $\lceil x \rceil$ " means the smallest integer  $\geq x$ , and for a divisor  $D = \sum d_i F_i$  :  $\lceil D \rceil = \sum \lceil d_i \rceil F_i$ .

This theorem is motivated by and used in the extremological program of *Miles Reid* for the construction of minimal models.

Reviewer: [V.Iliev](#)

**MSC:**

- [14C20](#) Divisors, linear systems, invertible sheaves
- [14F25](#) Classical real and complex (co)homology in algebraic geometry
- [14E30](#) Minimal model program (Mori theory, extremal rays)

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Mori extremal rays; nef Cartier divisor; non-vanishing theorem

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