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Semiclassical analysis of low lying eigenvalues. I: Non-degenerate minima: Asymptotic expansions. (English) [Zbl 0526.35027](#)

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MSC:

35J10 Schrödinger operator, Schrödinger equation
35P05 General topics in linear spectral theory for PDEs
81Q15 Perturbation theories for operators and differential equations in quantum theory

Cited in **6** Reviews
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Keywords:

semiclassical analysis; low lying eigenvalues; non-degenerate minima; asymptotic expansions; Schrödinger operators with multiple wells; quadratic approximation

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