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Characterization of orthogonally additive operators on sequence spaces. (English)

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Let X be a real sequence space which is AK as well as FK and with the property that for all $t \in N$, $(x_k) \in X : \|(x_1, x_2, \dots, x_t, 0, 0, \dots)\| \leq \|(x_k)\|$, where $\|\cdot\|$ denotes the paranorm on X . Let, moreover Y be a paranormed space. A mapping $F : X \rightarrow Y$ is said to be orthogonally additive if $F(x + y) = F(x) + F(y)$ whenever $x_k y_k = 0$ for all $k \in N$, $x = (x_k)$, $y = (y_k)$.

The author characterizes the continuous orthogonally additive maps from X to Y as follows.

Theorem: $F : X \rightarrow Y$ is orthogonally additive *iff* :

$F(x) = \sum_k g(k, x_k)$ for $X = (x_d) \in X$ with $g(k, x_k) : N \times R \rightarrow Y$ such that:

i) $g(k, 0) = 0$ for all $k \in N$

ii) $g(k, \cdot)$ is continuous on R , for all k

iii) $P_g : X \rightarrow cs(Y)$, where $P_g(x) = (g(k, x_k))_k$

and $cs(Y) = \{(y_n); y_n \in Y, \text{ for all } n, \text{ and } \sum_n y_n \in Y\}$.

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MSC:

46A45 Sequence spaces (including Köthe sequence spaces)

47B37 Linear operators on special spaces (weighted shifts, operators on sequence spaces, etc.)

Cited in 1 Review

Keywords:

paranormed space; continuous orthogonally additive maps