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**Singular points of the sum of a Dirichlet series on the convergence line.** (English. Russian original) [Zbl 1325.30002](#)

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Summary: We study the distribution of singular points of the sum of a Dirichlet series and obtain necessary and sufficient conditions for the sum of such a series to have at least one singular point on any segment of given length on the convergence line.

**MSC:**

**30B50** Dirichlet series, exponential series and other series in one complex variable

Cited in **5** Documents

**Keywords:**

Dirichlet series; singular points

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**References:**

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