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Breaking cycle structure to improve lower bound for Max-SAT. (English) [Zbl 07048079](#)

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Summary: Many practical optimization problems can be translated to Max-SAT and solved using a Branch-and-Bound (BnB) Max-SAT solver. The performance of a BnB Max-SAT solver heavily depends on the quality of the lower bound. Lower bounds in state-of-the-art BnB Max-SAT solvers are based on detecting inconsistent subsets of clauses and then on applying Max-SAT resolution to transform each inconsistent subset of clauses into an equivalent set containing an empty clause and a number of compensation clauses. In this paper, we focus on the transformation of the inconsistent subsets of clauses containing one unit clause and a number of binary clauses. We show that Max-SAT resolution generates a lot of ternary compensation clauses when transforming such an inconsistent set, deteriorating the quality of the lower bound, and propose a new inference rule, called cycle breaking rule, to transform the inconsistent set. We prove the correctness of the rule and implement it in a new BnB Max-SAT solver called Brmaxsat. Experimental results showed that cycle breaking rule is very effective, especially on Max-2SAT.

For the entire collection see [\[Zbl 1407.68047\]](#).

MSC:

[68Wxx](#) Algorithms in computer science

Keywords:

[NP-complete](#); [Max-SAT](#); [branch and bound](#); [lower bound](#)

Software:

[CCLS](#); [MaxHS](#); [UBCSAT](#)

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References:

- [1] Cook, S.A.: The complexity of theorem proving procedures. In: *Proceedings of the 3rd Annual ACM Symposium on Theory of Computing*, Shaker Heights, pp. 151–158 (1971)
- [2] Zhang, L., Madigan, C.F., Moskewicz, M.H., Malik, S.: Efficient conflict driven learning in a boolean satisfiability solver. In: *Proceedings of IEEE/ACM International Conference on Computer-Aided Design, ICCAD 2001*, pp. 279–285 (2001)
- [3] Anstegui, C., Bonet, M.L., Levy, J.: SAT-based MaxSAT algorithms. *Artif. Intell.* 196, 77–105 (2013) · [Zbl 1270.68265](#)
- [4] Davies, J., Bacchus, F.: Postponing optimization to speed up MAXSAT solving. In: Schulte, C. (ed.) *CP 2013. LNCS*, vol. 8124, pp. 247–262. Springer, Heidelberg (2013)
- [5] Gaspers, S., Sorkin, G.B.: A universally fastest algorithms for Max 2-Sat, Max 2-CSP, and everything in between. *J. Comput. Syst. Sci.* 78, 305–335 (2012) · [Zbl 1238.68066](#)
- [6] Davis, M., Logemann, G., Loveland, D.: A machine program for theorem proving. *Commun. ACM* 5(7), 394–397 (1962) · [Zbl 0217.54002](#)
- [7] Kuegel, A.: Improved exact solver for the weighted MAXSAT problem. In: *Workshop Pragmatics of SAT, Edinburgh, Scotland (2010)*
- [8] Argelich, J., Li, C.-M., Manyà, F.: An improved exact solver for partial Max-SAT. In: *Proceedings of International Conference on Non-convex Programming: Local and Global Approaches*, pp. 230–231 (2007)
- [9] Liu, Y.-L., Li, C.-M., He, K.: Improved lower bounds in MAXSAT complete algorithm based optimizing inconsistent set. *Chin. J. Comput.* 10(36), 2087–2096 (2013)
- [10] Abram, A., Habet, D.: On the resiliency of unit propagation to maxresolution. In: *Proceedings of the 24th International Joint Conference on Artificial Intelligence (IJCAI 2015)*, pp. 268–274 (2015)
- [11] Anstegui, C., Malitsky, Y., Sellmann, M.: Max-SAT by Improved instance-specific algorithm configuration. In: *Proceedings*

of the 28th National Conference on Artificial Intelligence (AAAI 2014), pp. 2594–2600 (2014)

- [12] Tompkins, D.A.D., Hoos, H.H.: UBCSAT: an implementation and experimentation environment for SLS algorithms for SAT and MAX-SAT. In: Hoos, H.H., Mitchell, D.G. (eds.) SAT 2004. LNCS, vol. 3542, pp. 306–320. Springer, Heidelberg (2005) · [Zbl 1122.68620](#)
- [13] Wallace, R., Freuder, E.: Comparative studies of constraint satisfaction and Davis-Putnam algorithms for maximum satisfiability problems. In: Johnson, D., Trick, M. (eds.) Cliques, Coloring and Satisfiability, vol. 26, pp. 587–615. American Mathematical Society, Providence (1996) · [Zbl 0859.68072](#)
- [14] Shen, H., Zhang, H.: Study of lower bound functions for MAX-2SAT. In: Proceedings of the 19th National Conference on Artificial Intelligence (AAAI 2004), pp. 185–190 (2004)
- [15] Li, C.-M., Manyà, F., Planes, J.: Exploiting unit propagation to compute lower bounds in branch and bound Max-SAT solvers. In: van Beek, P. (ed.) CP 2005. LNCS, vol. 3709, pp. 403–414. Springer, Heidelberg (2005) · [Zbl 1153.68470](#)
- [16] Li, C.-M., Manyà, F., Planes, J.: New inference rules for Max-SAT. *J. Artif. Intell. Res.* 30, 321–329 (2007) · [Zbl 1182.68254](#)
- [17] Li, C.M., Manyà, F., Mohamedou, N., Planes, J.: Exploiting cycle structures in Max-SAT. In: Kullmann, O. (ed.) SAT 2009. LNCS, vol. 5584, pp. 467–480. Springer, Heidelberg (2009) · [Zbl 1247.68256](#)
- [18] Li, C.-M., Manyà, F., Mohamedou, N., Planes, J.: Resolution-based lower bounds in MaxSAT. *Constraints* 15(4), 456–484 (2010) · [Zbl 1208.68204](#)
- [19] Bonet, M.L., Levy, J., Manyà, F.: Resolution for Max-SAT. *Artif. Intell.* 171, 606–618 (2007) · [Zbl 1168.68541](#)
- [20] Luo, C., Cai, S., Wu, W., Jie, Z., Su, K.: CCLS: an efficient local search algorithm for weighted maximum satisfiability. *IEEE Trans. Comput.* 64(7), 1830–1843 (2015) · [Zbl 1360.68786](#)
- [21] Bansal, N., Raman, V.: Upper bounds for MaxSat: further improved. In: Aggarwal, A.K., Pandu Rangan, C. (eds.) ISAAC 1999. LNCS, vol. 1741, pp. 247–258. Springer, Heidelberg (1999) · [Zbl 0971.68069](#)
- [22] Niedermeier, R., Rossmanith, P.: New upper bounds for maximum satisfiability. *J. Algorithms* 36, 63–88 (2000) · [Zbl 0959.68049](#)
- [23] <http://www.maxsat.udl.cat/index.html>

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