Pin, Jean-Eric

Tropical semirings. (English) Zbl 0909.16028

Gunawardena, Jeremy (ed.), Idempotency. Based on a workshop, Bristol, UK, October 3-7, 1994, Cambridge: Cambridge University Press. 50-69 (1998).

The paper is a brief self-contained introduction in some decidability problems for sets of matrices over semirings $(k, +, \cdot)$ as well as in such problems for rational languages. The connection between both types of problems comes from the matrix representation of k-automata which serve as recognizers for the languages. Here a semiring is always an additively commutative one with absorbing zero and identity. Moreover, in most results which are cited, $(k, +, \cdot)$ is a tropical semiring, i.e., $k = \mathbb{N} \cup \{\infty\}$ or $k = \mathbb{Z} \cup \{\infty\}$ or $k = \mathbb{R} \cup \{\infty\}$ or similar, and $a + b = \min(a, b)$ and $a \cdot b = a + b$, the latter in the usual meaning on the particular set k. The problems under consideration are: Burnside problem, finiteness problem, finite section problem, finite power property problem, polynomial closure problem.

For the entire collection see [Zbl 0882.00035].

Reviewer: U.Hebisch (Freiberg)

MSC:

68Q45

16Y60 Semirings Cited in 44 Documents

Formal languages and automata Algebraic theory of languages and automata 68Q70

20M35 Semigroups in automata theory, linguistics, etc.

Keywords:

semirings; rational languages; decidability problems; Burnside problem; automata

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