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Epstein zeta function and Bloch-Wigner dilogarithm. (Fonction zêta d'Epstein et dilogarithme de Bloch-Wigner.) (French. English summary) Zbl 1278.11072

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Summary: We give an expression for $s = 2$ of some normalized Epstein series as Bloch-Wigner dilogarithms of algebraic numbers of $\mathbb{Q}(\sqrt{\Delta})$, for the discriminants Δ associated to the quadratic form.

MSC:

11G55 Polylogarithms and relations with K-theory
11E45 Analytic theory (Epstein zeta functions; relations with automorphic forms and functions)
11R42 Zeta functions and L-functions of number fields

Keywords:

Epstein series; Bloch-Wigner dilogarithm; Dirichlet L-series; Bloch groups of number fields

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